
Necht' f a g jsou funkce, $c \in \mathbb{R}$.

- $(f \pm g)' = f' \pm g'$,
- $(c \cdot f)' = c \cdot f'$,
- $[f(g(x))]' = f'(g(x)) \cdot g'(x)$,
- $(f \cdot g)' = f'g + fg'$,
- $\left(\frac{f}{g}\right)' = \frac{f'g - fg'}{g^2}$.

Necht' $a, b, c, \alpha \in \mathbb{R}$ ($a, b > 0, \alpha \neq 0, b \neq 1$).

- $(c)' = 0$,
- $(x^\alpha)' = \alpha x^{\alpha-1}$,
- $(e^x)' = e^x$,
- $(a^x)' = a^x \cdot \ln a$,
- $(\ln x)' = \frac{1}{x}$,
- $(\log_b x)' = \frac{1}{x \cdot \ln b}$,
- $(\sin x)' = \cos x$,
- $(\cos x)' = -\sin x$,
- $(\operatorname{tg} x)' = \frac{1}{\cos^2 x}$,
- $(\operatorname{cotg} x)' = \frac{-1}{\sin^2 x}$,
- $(\arcsin x)' = \frac{1}{\sqrt{1-x^2}}$,
- $(\arccos x)' = \frac{-1}{\sqrt{1-x^2}}$,
- $(\operatorname{arctg} x)' = \frac{1}{1+x^2}$,
- $(\operatorname{arccotg} x)' = \frac{-1}{1+x^2}$.

Necht' $A, B, a, c, k, n \in \mathbb{R}$ ($A, B \neq 0, a > 0, a \neq 1, n \neq -1$).

- $\int k \, dx = kx + c$,
- $\int x^n \, dx = \frac{x^{n+1}}{n+1} + c$,
- $\int \frac{1}{x} \, dx = \ln|x| + c$,
- $\int a^x \, dx = \frac{a^x}{\ln a} + c$,
- $\int e^x \, dx = e^x + c$,
- $\int \sin x \, dx = -\cos x + c$,
- $\int \cos x \, dx = \sin x + c$,
- $\int \frac{1}{\cos^2 x} \, dx = \operatorname{tg} x + c$,
- $\int \frac{1}{\sin^2 x} \, dx = -\operatorname{cotg} x + c$,
- $\int \frac{1}{\sqrt{A^2-x^2}} \, dx = \arcsin \frac{x}{A} + c$,
- $\int \frac{1}{\sqrt{x^2 \pm B}} \, dx = \ln|x + \sqrt{x^2 \pm B}| + c$,
- $\int \frac{1}{A^2+x^2} \, dx = \frac{1}{A} \operatorname{arctg} \frac{x}{A} + c$,
- $\int \frac{1}{A^2-x^2} \, dx = \frac{1}{2A} \ln \left| \frac{A+x}{A-x} \right| + c$.

Necht' f a g jsou funkce, $k, c \in \mathbb{R}$.

- $\int [f(x) \pm g(x)] \, dx = \int f(x) \, dx \pm \int g(x) \, dx$,
- $\int k \cdot f(x) \, dx = k \cdot \int f(x) \, dx$,
- $\int \frac{f'(x)}{f(x)} \, dx = \ln|f(x)| + c$.

Necht' F je primitivní funkce k funkci f ($a, b \in \mathbb{R}$).

- $\int_a^b f(x) \, dx = F(b) - F(a)$.

Integrovaní per partes [$u = u(x), v = v(x)$].

$$\int uv' \, dx = uv - \int u'v \, dx.$$

Substituční metoda.

$$\int f(x) \, dx = \left| \begin{array}{l} x = h(t) \\ dx = h'(t) \, dt \end{array} \right| = \int f(h(t))h'(t) \, dt,$$

$$\int f(g(x))g'(x) \, dx = \left| \begin{array}{l} g(x) = t \\ g'(x) \, dx = dt \end{array} \right| = \int f(t) \, dt.$$

Délka křivky.

$$\ell = \int_a^b \sqrt{1 + f'^2(x)} \, dx.$$

Povrch pláště a objem rotačního tělesa (rotace f kolem osy x).

$$P = 2\pi \int_a^b f(x) \sqrt{1 + f'^2(x)} \, dx,$$

$$V = \pi \int_a^b f^2(x) \, dx.$$
