

## Definition 2.1 (Excellent number)

Let  $n$  be positive integer. The number  $n$  is said to be *excellent*, if the last digit of the number  $\alpha$  defined by the relation

$$\alpha = n^2 + \int_0^{2\pi} \sin x dx \quad (1)$$

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## Definition 2.2 (Happy number)

Let  $n$  be positive integer. The number  $n$  is said to be *happy*, if the last digit of the number  $n$  equals 1.

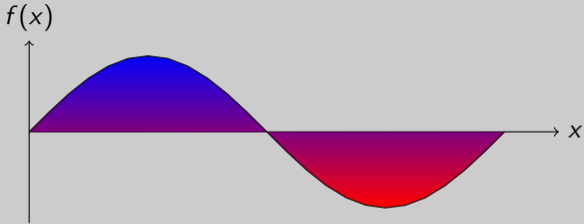


Figure: Sine curve

## Theorem 2.4

*Let  $f(x)$  be integrable in the sense of Riemann on  $[a, b]$ . Let  $F(x)$  be a function continuous on  $[a, b]$  which is an antiderivative of the function  $f$  on the interval  $(a, b)$ . Then*

$$\int_a^b f(x)dx = [F(x)]_a^b = F(b) - F(a)$$

*holds.*

$$\int_0^{2\pi} \sin x dx = 0. \quad (2)$$

## Theorem 2.5 (Characterization of excellent numbers)

*The positive integer  $n$  is excellent if and only if the last digit of the number  $n$  is either 1 or 9.*